

ExoEarth Target Lists
How Many Stars Need to be Searched?
How Large a Telescope is Needed?

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Background

- Want the mission to have a positive result.
 - Find an Earth with >95% probability
 - On average find 3 Earths
- What is an Earth clone?
 - $0.5 \sim 10 M_{\text{Earth}}$? (but $> 5 M_{\text{Earth}}$ the planet can have a hydrogen atmos)
 - $0.7 \sim 1.8 \text{ AU} \cdot \sqrt{\text{Lum}}$? Colder than Mars,
- How many Earths are there? (Catanzarite, Shao) $\sim 3\%$ of solar like stars have Earths.
- Should we include wide doubles? (double stars are now known to have planets) Include doubles unless there is a Jupiter between $0.2 \sim 5 \text{ yr}$ period?
 - Astrometry (unlike coronagraph) has no problem with wide doubles. In fact the search time is halved.

Background 2

- How a question is asked changes what the correct answer is.
 - If we assume that every star either has 1 Earth or 0 Earths in the HZ and **no other planets**, that assumption provides a strong constraint on what search techniques can work.
 - External occulter (starshades) are very limited in the number of targets they can look at. But with the above assumption a single detection of a dot, is proof that an Earth has been found. If one assumes every planet is Earth mass(or size) and every planet is in the habitable zone, then any detection of a planet is a detection of an Earth.
 - Brightness of a planet (in reflected light) can change by a factor of 10 depending on phase angle. Angular separation can also change 10X depending on orbit inclination and orbit phase. A Neptune @ 4 AU can have the same brightness and apparent angular separation as Earth at 1AU.

Scaling Laws for Photon Limited Astrometric Detection of Exoplanets

- If the field of view (FOV) is held constant (eg ~ 0.5 deg dia)
 - Accuracy goes as Dia^{-2}
 - Integration time to reach XX uas precision goes as Dia^{-4}
 - # stars increases as Dist^3
 - Astrometric signal goes as Dist^{-1}
 - Integration time as Dist^2
- If our final accuracy is limited (by Dia^{-1}) but not obs time
 - # targets grows Diameter^3
- If we totally photon and mission time limited and accuracy goes as Dia^{-2}
 - 2X increase in distance \Rightarrow 8X as many targets
 - But each target has $\frac{1}{2}$ the astrometric signature \Rightarrow 4X integ time per target \Rightarrow total 32X increase in mission time.
 - Compensate with Dia that is 2.3X larger.
 - #targets $\sim \text{Dia}^{2.4}$, 1.34m NEAT \Rightarrow 2X as many Earths (~ 200)
- If $\text{Eta}_{\text{Earth}}$ is **30%**, a **37cm dia NEAT** would have a 95% chance of finding 1 Earth. If $\text{Eta}_{\text{Earth}}$ is **3%**, **Dia \sim 1m**

Narrow Angle Astrometry is not Necessarily 1 mission

- Astrometry at <10uas has to be done from space
- From 40cm telescope to 2.0m telescope (with 0.6deg Dia FOV) represents a wide range of accuracy & # of targets as well as cost
 - 40cm ~ search 10 stars to 1 Me, (or ~40 stars to 2 Me) (10% of cost of \$ NEAT assuming \$\$ = ~ D^{2.5})
 - 1m (default NEAT) ~100 stars at a cost of ESA M mission
 - 2m version ~ 500 stars to 1 Me, \$\$~ 5.5X Neat cost
- A version that can “drain the lake” at 100pc, would be **very** expensive.
 - ~10,000 stars down 1 Me, (in a 5yr mission) ~ 5 m telescope. But even if eta_Earth is 3%, this would produce ~300 Earths.